

CLASS: PHY _____

STUDENT #: _____

NAME: _____

Assignment 9: Ideal Gas Equation First Law of Thermodynamics

Assigned: Monday Nov 14 Due: Monday Nov 21 19:00

1 An automobile tire is inflated with air originally at 10.0°C and normal atmospheric pressure. During the process, the air is compressed to 28.0% of its original volume and the temperature is increased to 40.0°C. (a) What is the tire pressure? (b) After the car is driven at high speed, the tire air temperature rises to 85.0°C and the interior volume of the tire increases by 2.00%. What is the new tire pressure (absolute) in pascals?

(a) Initially, $P_i V_i = n_i R T_i$ $(1.00 \text{ atm}) V_i = n_i R (10.0 + 273.15) \text{ K}$
 Finally, $P_f V_f = n_f R T_f$ $P_f (0.280 V_i) = n_i R (40.0 + 273.15) \text{ K}$
 Dividing these equations, $\frac{0.280 P_f}{1.00 \text{ atm}} = \frac{313.15 \text{ K}}{283.15 \text{ K}}$
 giving $P_f = 3.95 \text{ atm}$
 or $P_f = \boxed{4.00 \times 10^5 \text{ Pa (abs)}}$.
 (b) After being driven $P_d (1.02) (0.280 V_i) = n_i R (85.0 + 273.15) \text{ K}$
 $P_d = 1.121 P_f = \boxed{4.49 \times 10^5 \text{ Pa}}$

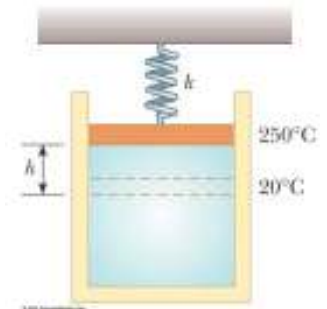
2 Just 9.00 g of water is placed in a 2.00-L pressure cooker and heated to 500°C. What is the pressure inside the container?

water contributes $P = \frac{nRT}{V} = \left(\frac{9.00 \text{ g}}{18.0 \text{ g/mol}} \right) \left(\frac{8.314 \text{ J}}{\text{mol K}} \right) \left(\frac{773 \text{ K}}{2.00 \times 10^{-3} \text{ m}^3} \right) = \boxed{1.61 \text{ MPa}} = 15.9 \text{ atm}$

air contributes $P_{\text{air}} = \frac{nRT}{V} = \left(\frac{21}{22.41} \right) \text{ mol} \frac{8.314 \text{ J}}{\text{mol K}} \left(\frac{773 \text{ K}}{2 \times 10^{-3} \text{ m}^3} \right) = 286769.2 \text{ Pa} = 2.83 \text{ atm}$

SUM IS THE CORRECT ANSWER 18.73 atm.

A cylinder is closed by a piston connected to a spring of constant $2.00 \times 10^3 \text{ N/m}$ (see Fig. P19.50). With the spring relaxed, the cylinder is filled with 5.00 L of gas at a pressure of 1.00 atm and a temperature of 20.0°C. (a) If the piston has a cross-sectional area of 0.010 0 m² and negligible mass, how high will it rise when the temperature is raised to 250°C? (b) What is the pressure of the gas at 250°C?



(a) $\frac{P_0 V}{T} = \frac{P' V'}{T'}$
 $V' = V + A h$
 $P' = P_0 + \frac{k h}{A}$
 $\left(P_0 + \frac{k h}{A} \right) (V + A h) = P_0 V \left(\frac{T'}{T} \right)$
 $\left(1.013 \times 10^5 \text{ N/m}^2 + 2.00 \times 10^5 \text{ N/m}^3 h \right)$
 $\left(5.00 \times 10^{-3} \text{ m}^3 + (0.0100 \text{ m}^2) h \right)$
 $= \left(1.013 \times 10^5 \text{ N/m}^2 \right) \left(5.00 \times 10^{-3} \text{ m}^3 \right) \left(\frac{523 \text{ K}}{293 \text{ K}} \right)$
 $2000h^2 + 2013h - 397 = 0$
 $h = \frac{-2013 \pm 2689}{4000} = \boxed{0.169 \text{ m}}$

(b) $P' = P + \frac{k h}{A} = 1.013 \times 10^5 \text{ Pa} + \frac{(2.00 \times 10^3 \text{ N/m})(0.169)}{0.0100 \text{ m}^2} P' = \boxed{1.35 \times 10^5 \text{ Pa}}$

4. An aluminum calorimeter with a mass of 100 g contains 250 g of water. The calorimeter and water are in thermal equilibrium at 10.0°C. Two metallic blocks are placed into the water. One is a 50.0-g piece of copper at 80.0°C. The other block has a mass of 70.0 g and is originally at a temperature of 100°C. The entire system stabilizes at a final temperature of 20.0°C. (a) Determine the specific heat of the unknown sample. (b) Guess the material of the unknown, using the data in Table 20.1.

(a) $Q_{\text{cold}} = -Q_{\text{hot}}$
 $(m_w c_w + m_c c_c)(T_f - T_c) = -m_{\text{Cu}} c_{\text{Cu}}(T_f - T_{\text{Cu}}) - m_{\text{unk}} c_{\text{unk}}(T_f - T_{\text{unk}})$
 where w is for water, c the calorimeter, Cu the copper sample, and unk the unknown.
 $[250 \text{ g}(1.00 \text{ cal/g} \cdot ^\circ\text{C}) + 100 \text{ g}(0.215 \text{ cal/g} \cdot ^\circ\text{C})](20.0 - 10.0)^\circ\text{C}$
 $= -(50.0 \text{ g})(0.0924 \text{ cal/g} \cdot ^\circ\text{C})(20.0 - 80.0)^\circ\text{C} - (70.0 \text{ g}) c_{\text{unk}}(20.0 - 100)^\circ\text{C}$
 $2.44 \times 10^3 \text{ cal} = (5.60 \times 10^3 \text{ g} \cdot ^\circ\text{C}) c_{\text{unk}}$
 or $c_{\text{unk}} = \boxed{0.435 \text{ cal/g} \cdot ^\circ\text{C}}$.

(b) The material of the sample is beryllium.

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Assignment 9: CONT

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5. A 1.00-kg block of copper at 20.0°C is dropped into a large vessel of liquid nitrogen at 77.3 K. How many kilograms of nitrogen boil away by the time the copper reaches 77.3 K? (The specific heat of copper is 0.092 0 cal/g·°C. The latent heat of vaporization of nitrogen is 48.0 cal/g.)

$$Q = m_{\text{Cu}} c_{\text{Cu}} \Delta T = m_{\text{N}_2} (L_{\text{vap}})_{\text{N}_2}$$

$$1.00 \text{ kg} (0.092 0 \text{ cal/g} \cdot ^\circ\text{C}) (293 - 77.3) ^\circ\text{C} = m (48.0 \text{ cal/g})$$

$$m = \boxed{0.414 \text{ kg}}$$

6. (a) Determine the work done on a fluid that expands from i to f as indicated in Figure (b) How much work is performed on the fluid if it is compressed from f to i along the same path?

(a) $W = -\int P dV$

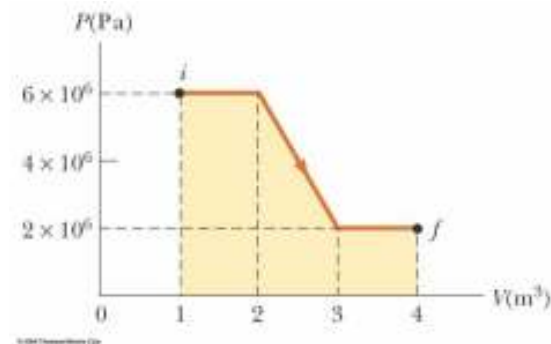
$$W = -\left(6.00 \times 10^6 \text{ Pa}\right)(2.00 - 1.00) \text{ m}^3 +$$

$$-\left(4.00 \times 10^6 \text{ Pa}\right)(3.00 - 2.00) \text{ m}^3 +$$

$$-\left(2.00 \times 10^6 \text{ Pa}\right)(4.00 - 3.00) \text{ m}^3$$

$$W_{i \rightarrow f} = \boxed{-12.0 \text{ MJ}}$$

(b) $W_{f \rightarrow i} = \boxed{+12.0 \text{ MJ}}$



7. A sample of an ideal gas goes through the process shown in Figure P20.32. From A to B , the process is adiabatic; from B to C , it is isobaric with 100 kJ of energy entering the system by heat. From C to D , the process is isothermal; from D to A , it is isobaric with 150 kJ of energy leaving the system by heat. Determine the difference in internal energy $E_{\text{int},B} - E_{\text{int},A}$.

$$W_{BC} = -P_B (V_C - V_B) = -3.00 \text{ atm} (0.400 - 0.090 0) \text{ m}^3$$

$$= -94.2 \text{ kJ}$$

$$\Delta E_{\text{int}} = Q + W$$

$$E_{\text{int},C} - E_{\text{int},B} = (100 - 94.2) \text{ kJ}$$

$$E_{\text{int},C} - E_{\text{int},B} = 5.79 \text{ kJ}$$

Since T is constant,

$$E_{\text{int},D} - E_{\text{int},C} = 0$$

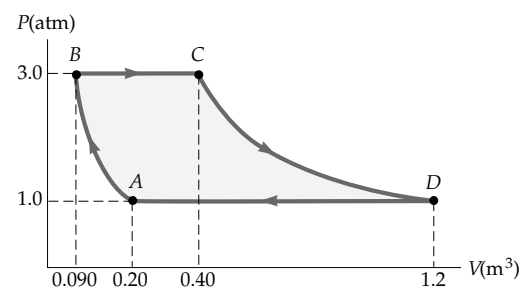
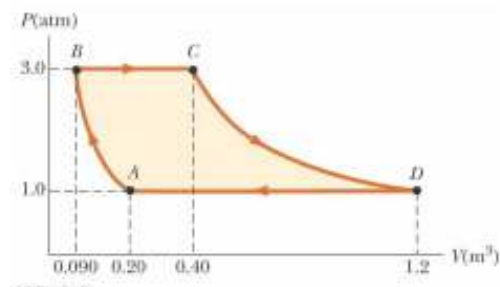
$$W_{DA} = -P_D (V_A - V_D) = -1.00 \text{ atm} (0.200 - 1.20) \text{ m}^3$$

$$= +101 \text{ kJ}$$

$$E_{\text{int},A} - E_{\text{int},D} = -150 \text{ kJ} + (+101 \text{ kJ}) = -48.7 \text{ kJ}$$

Now,

$$E_{\text{int},B} - E_{\text{int},A} = -\left[(E_{\text{int},C} - E_{\text{int},B}) + (E_{\text{int},D} - E_{\text{int},C}) + (E_{\text{int},A} - E_{\text{int},D})\right]$$



8. Assume that the Earth's atmosphere has a uniform temperature of 20°C and uniform composition, with an effective molar mass of 28.9 g/mol. (a) Show that the number density of molecules depends on height according to

$$n_V(y) = n_0 e^{-mgy / k_B T}$$

where n_0 is the number density at sea level, where $y = 0$. This result is called the *law of atmospheres*. (b) Commercial jetliners typically cruise at an altitude of 11.0 km. Find the ratio of the atmospheric density there to the density at sea level.

SOLUTION:

(a) Consult the lecture notes from Nov 22/Nov21

(b) $\frac{n(y)}{n_0} = e^{-mgy / k_B T} = e^{-Mgy / N_A k_B T} = e^{-Mgy / RT}$

$$= e^{-\left(28.9 \times 10^{-3} \text{ kg/mol}\right)\left(9.8 \text{ m/s}^2\right)\left(11 \times 10^3 \text{ m}\right) / \left(8.314 \text{ J/mol} \cdot \text{K}\right)(293 \text{ K})}$$

$$= e^{-1.279} = \boxed{0.278}$$